

$$180 = 0.01746 \times 180 = 0.01746$$

$$1^\circ = 0.01746$$

$$268 \times 0.01746 = 268 \times 0.01746 = 4.679 \approx 4.68$$

$$\therefore 268^\circ = 4.68 \text{ radians}$$

2) Convert  $155^\circ$  to radians.

$$1^\circ = \frac{\pi}{180} \quad 155^\circ = 155 \times \frac{\pi}{180} = \frac{31\pi}{36}$$

$$\therefore 155^\circ = \frac{31\pi}{36}$$

3) Convert 5.2 radians to degrees.

$$1^\circ = 0.01746$$

$$= \frac{5.2 \times 1}{0.01746} = 297.8^\circ = 298^\circ$$

4) Convert  $\frac{5\pi}{6}$  radians to the nearest degrees

$$1^\circ = \frac{\pi}{180}$$

$$\frac{5\pi}{6} \div \frac{\pi}{180} = \frac{5\pi}{6} \times \frac{180}{\pi}$$

$$= \frac{5\pi}{6} \times \frac{180}{\pi}$$

$$= \frac{150\pi}{\pi} = 150^\circ$$

$$\therefore \frac{5\pi}{6} = 150^\circ$$

5)

$$s = r\theta$$

$$s = 5.7 \text{ cm}$$

$$r = ?$$

$$r = s/\theta$$

$$\theta = \left(123^\circ \times \frac{\pi}{180}\right) = 2.1476$$

$$r = \frac{5.7}{2.1476} = 2.65$$

$$\therefore r = 2.65 \text{ cm}$$

$$10) a) y = \cos \frac{3\pi}{5} x.$$

$$y = A \cos (bx + c).$$

$$\text{Period of a function} = \frac{2\pi}{|b|}$$

$b$  is the function of  $x$ .

$$|b| = \frac{3\pi}{5}$$

$$\text{Period (P)} = 2\pi \div \frac{3\pi}{5}$$

$$= \frac{2\pi \times 5}{3\pi} = \frac{10\pi}{3\pi} = \frac{10}{3} = 3.33$$

$$P = 3.33$$

$$b) y = \tan \frac{5\pi}{3} x$$

$$\text{Period (P) of a tangent function} = \frac{\pi}{|b|}$$

$$|b| = \frac{5\pi}{3} = \pi$$

$$\therefore P = \pi \div \frac{5\pi}{3} = \pi \times \frac{3}{5\pi} = \frac{3}{5}$$

$$P = \frac{3}{5}$$

$$c) y = \sin \frac{3}{2} x$$

$$\text{Period } P = \frac{2\pi}{|b|}$$

$$|b| = \frac{3}{2}$$

$$\therefore P = 2\pi \div \frac{3}{2} = 2\pi \times \frac{2}{3} = \frac{4\pi}{3}$$

$$\therefore P = \frac{4\pi}{3}$$

$$1/180 = 0.0055 \times \frac{3.142}{180} = 0.01746$$

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3) Convert 5.2 radians to degrees.

$$1^\circ = 0.01746$$

$$5.2 \times 0.01746 = 297.8^\circ = 298^\circ$$

4) Convert  $\frac{5\pi}{6}$  radians to the nearest degrees

$$1^\circ = \frac{\pi}{180}$$
$$\frac{5\pi}{6} \div \frac{\pi}{180} = \frac{5\pi}{6} \times \frac{180}{\pi} = \frac{150\pi}{\pi} = 150^\circ$$

$$\therefore \frac{5\pi}{6} = 150^\circ$$

5)  $s = r\theta$

$$s = 5.7 \text{ cm}$$

$$r = ?$$

$$\theta = \left(123^\circ \times \frac{\pi}{180}\right) = 2.1476$$

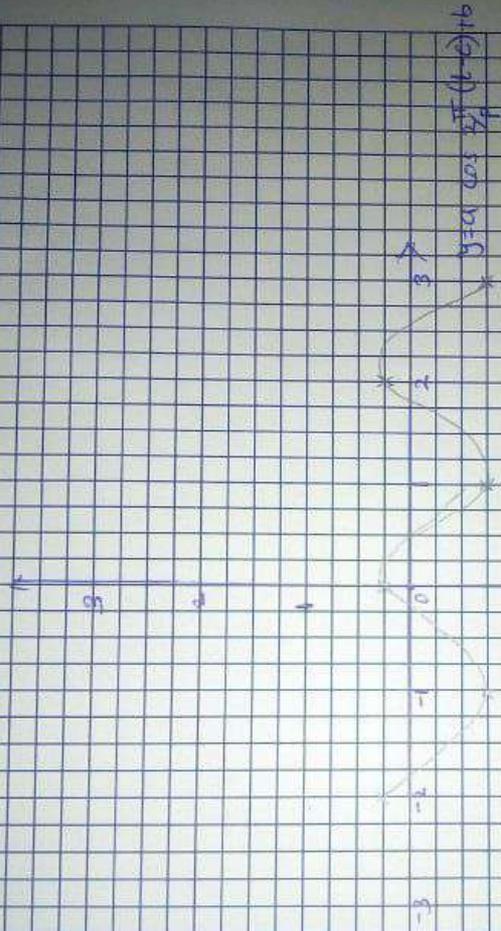
$$r = \frac{s}{\theta} = \frac{5.7}{2.1476} = 2.65$$

$$\therefore r = 2.65 \text{ cm}$$

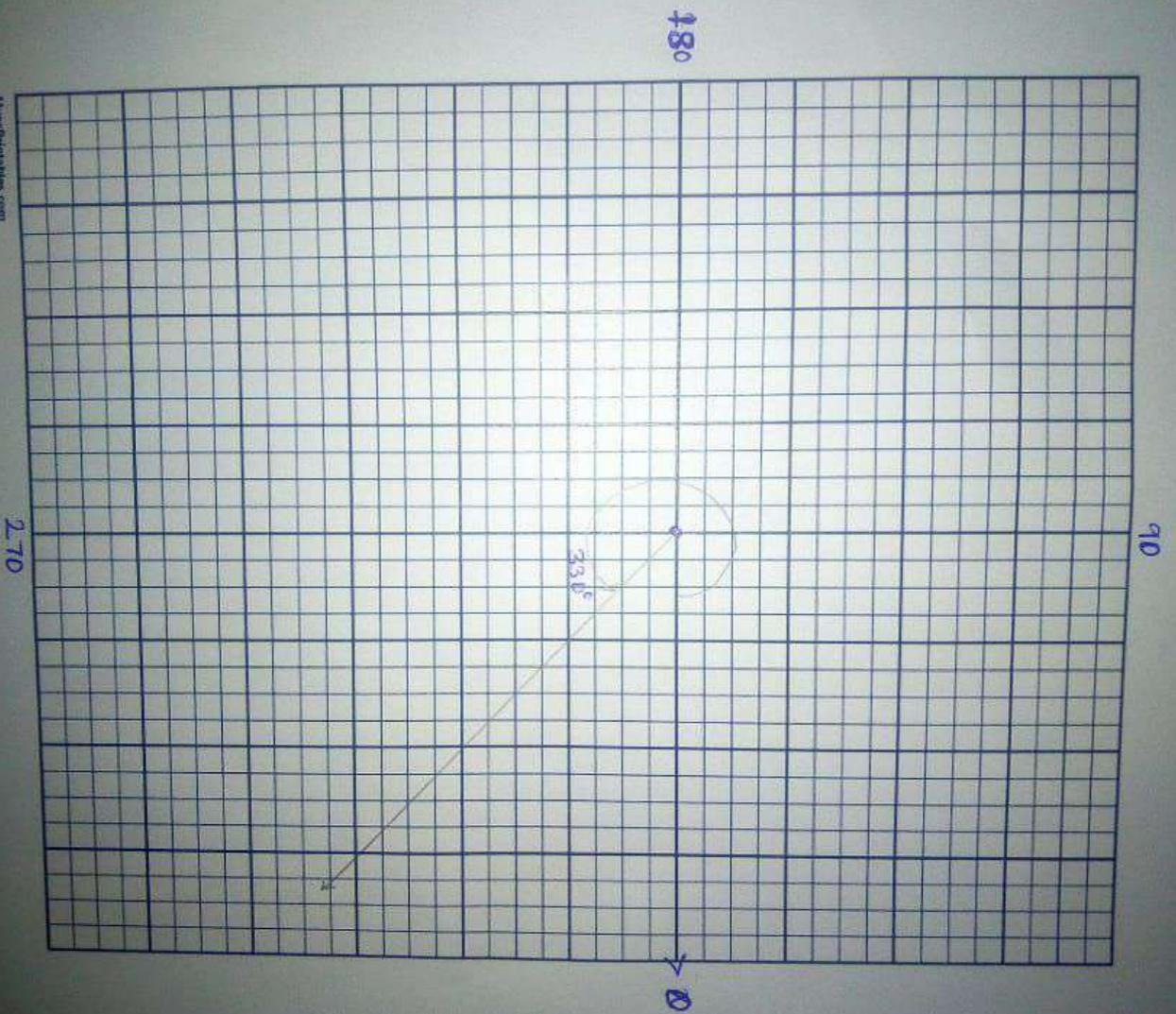
16.  $y = a \cos \frac{2\pi}{p} (t-c) + b$

$a$  = amplitude

$b$  = Vertical displacement







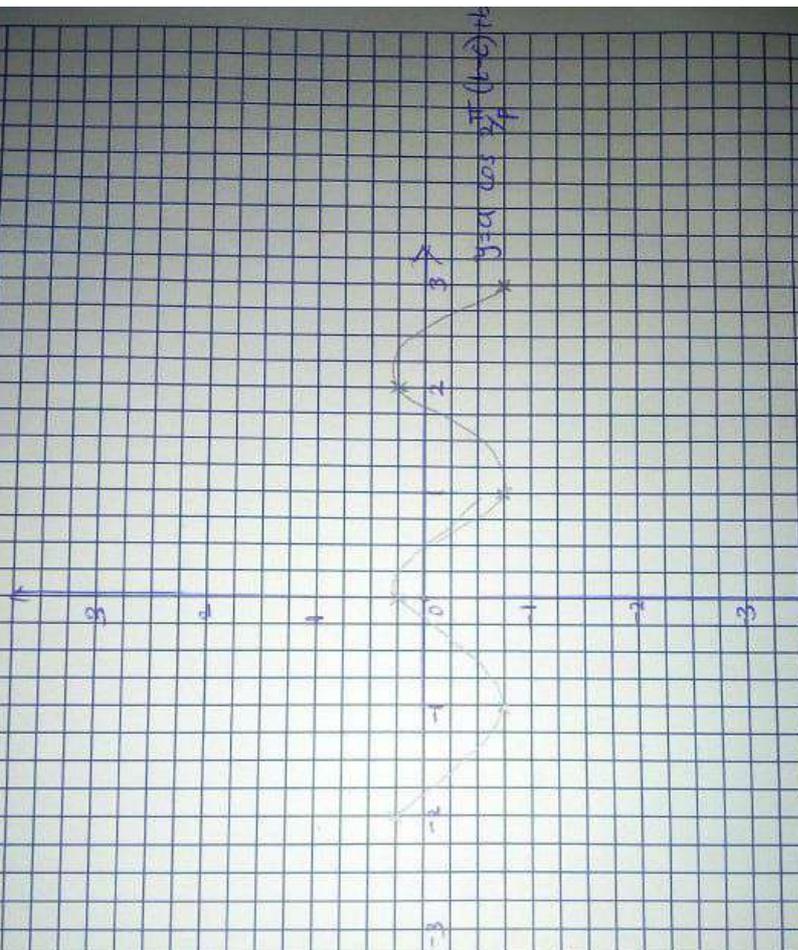
The reference angle is  $30^\circ$

The coterminal angle is  $360 - 330 = 30^\circ$

16.  $y = a \cos \frac{2\pi}{p}(t-c) + b$

$a$  = amplitude.

$b$  = Vertical displacement.



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$$y = A \sin (Bx + C) + D$$

$$C = -\pi$$

$$D = 0$$

$$A = 5$$

$$B = \frac{2\pi}{8} = \frac{\pi}{4}$$

$$\frac{2\pi}{\pi} = \frac{B \cdot \pi}{\pi}$$

$$B = 2$$

$$\therefore y = 5 \sin (2x - \pi)$$

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$$A = 4$$

$$B = -6$$

$$C = \frac{-\pi}{3} - \frac{2\pi}{3}$$

$$D = -2$$

$$\frac{2\pi}{8} = -\frac{\pi}{3}$$

$$\frac{2\pi}{8} = \frac{C \cdot \pi}{-\pi} = \frac{-\pi B}{-\pi}$$

$$-6B = -\pi$$

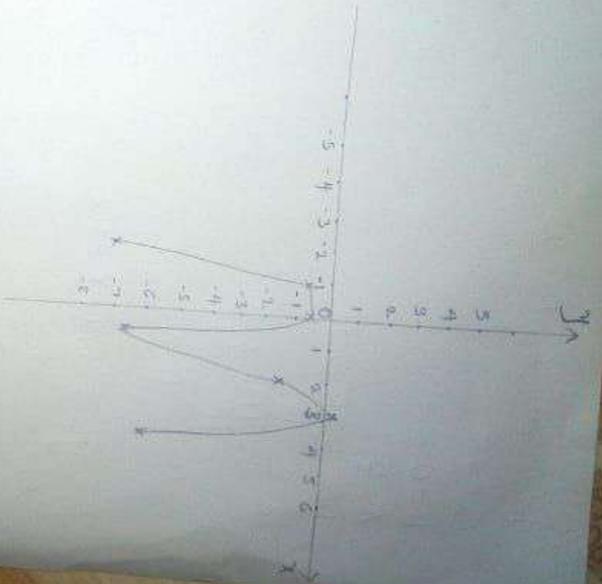
$$-6 = B$$

$$\therefore y = 4 \cos \left( -6x - \frac{2\pi}{3} \right) - 2$$

11)  $y = 4 \sin 2(x-5) - 3$

X	Y
-2	-7
-1	-0.84
0	-0.84
1	-0.96
2	-1.88
3	0.04
4	-0.96

Domain =  $(-\infty, \infty)$   
 Range =  $(-\infty, \infty)$



12)  $y = -3 \cos(2x + \pi/3) + 5$  determine;

amplitude

$y = a \cos(bx + c) + d$

$a$  is the amplitude.

$\therefore$  In our function our amplitude = ~~3~~ 3

Period

Period (P) =  $\frac{2\pi}{|b|} = \frac{2\pi}{2} = \pi$  ,  $|b| = 2$

$\therefore \frac{2\pi}{2} = P = \pi$

$P = \pi$

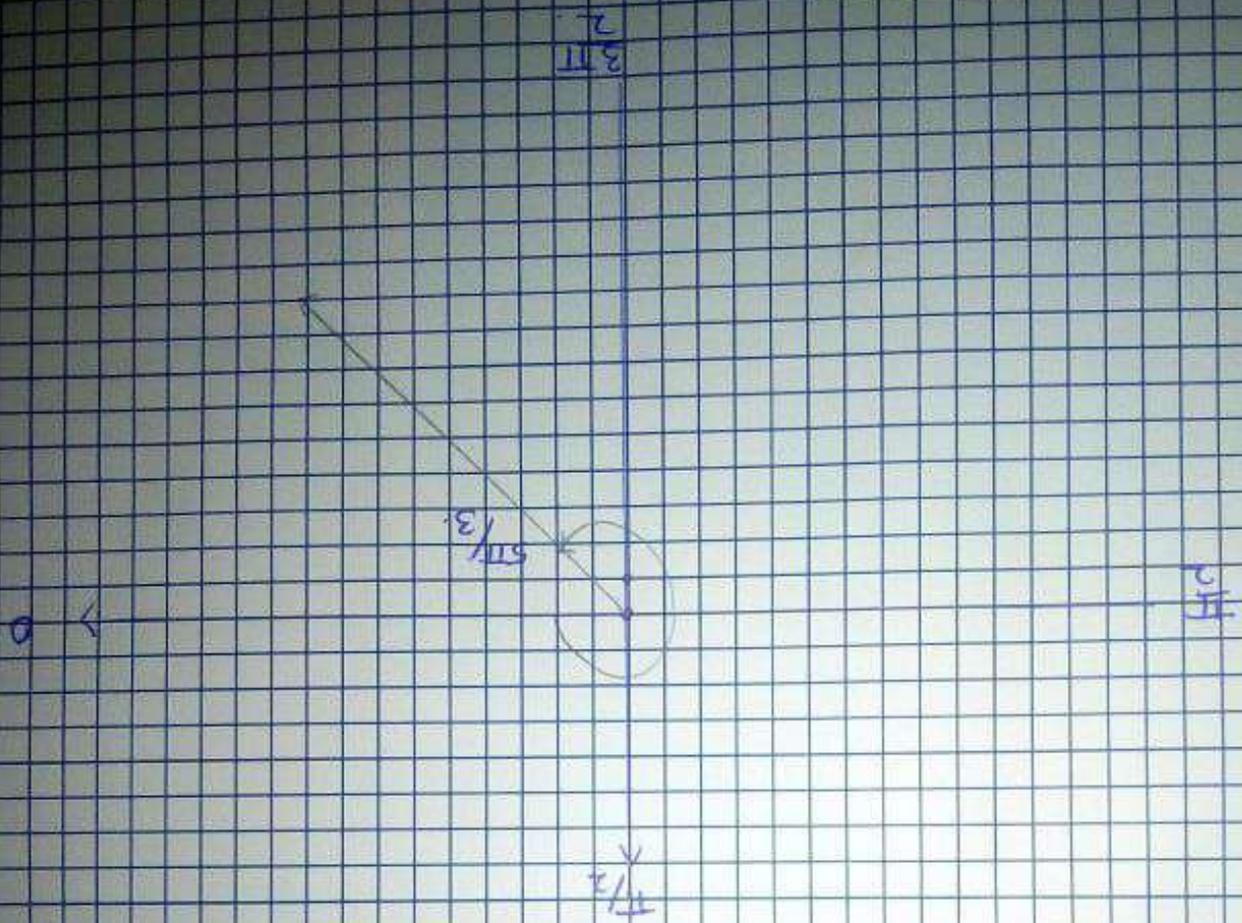
Phase shift =  $\frac{c}{b} = \frac{\pi/3}{2} = \frac{\pi}{6}$

Phase shift =  $\frac{\pi}{6}$

Vertical displacement =  $d = 5$

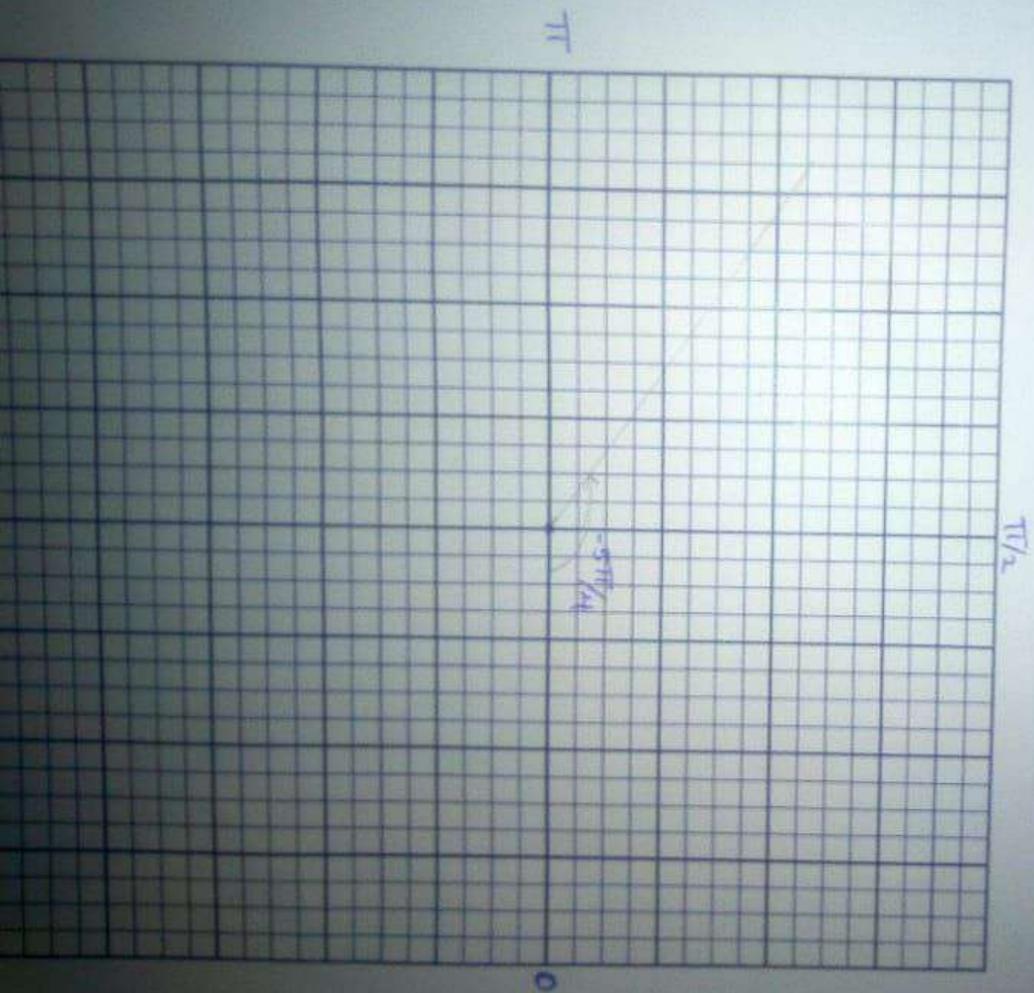
9. c)  $\sec \frac{5\pi}{3}$

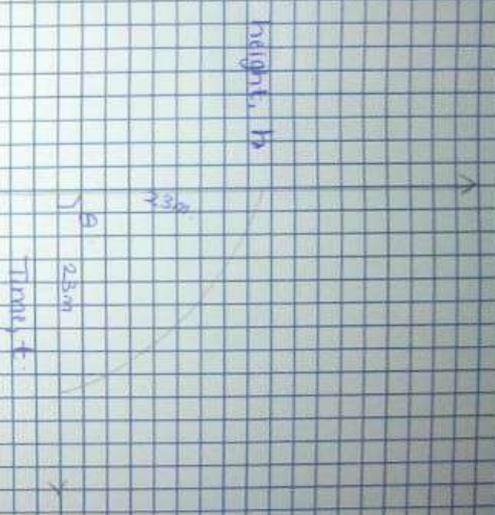
$$\cos \left( \frac{\pi}{3} \right) = \frac{1}{2} \quad \sec \left( \frac{11\pi}{3} \right) = 2$$



9b)  $\cos\left(-\frac{5\pi}{4}\right)$

$r = \frac{\pi}{180}$   
 $-\frac{5\pi}{4}$





b)  $\sin \theta = \frac{y_2}{y_3} = 0.08696$   
 $\sin^{-1} 0.08696 = 4.99^\circ$

c.  $h = 2.5m = 0$   
 $2m \times 2.5 = 50$   
 $= 50m$

d.  $2.5 \times 2 = 50m$   
 $= \frac{2.5 \times 4 \times 10^3}{50} = 200$   
 $= 200 \text{ sec}$

8) In the third quadrant, sine theta is negative while tan theta is positive. Thus,  $\sin \theta < 0$  and  $\tan \theta > 0$

$$7) \sin \theta = -\frac{7}{25} = -0.28$$

$$\sin^{-1} = -16.26^\circ$$

$$360 - 16.26 = 343.74^\circ$$

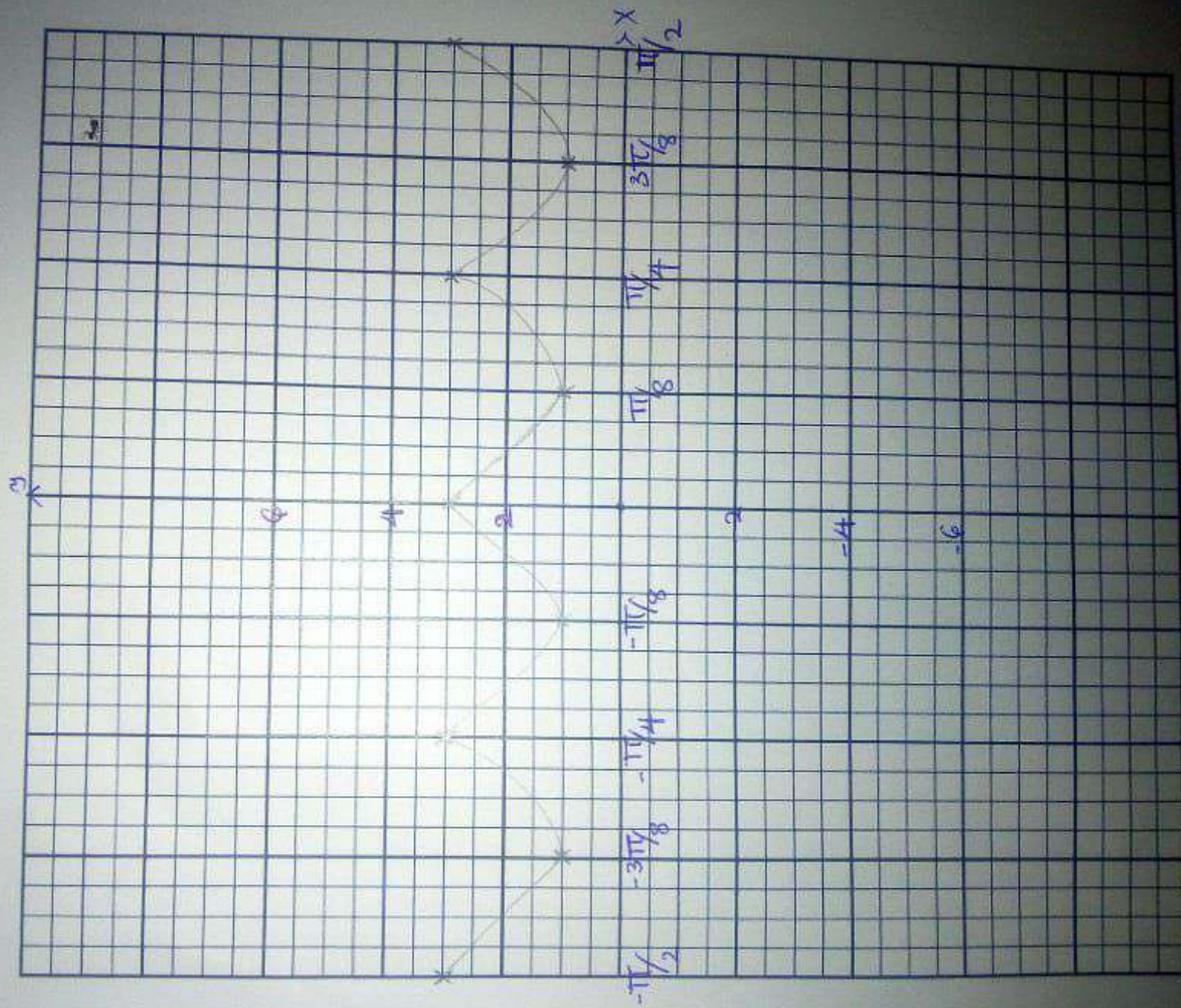
$\therefore$  The possible co-ordinate on the terminal arm of angle  $\theta$  is  
~~32~~  $16.26^\circ$ .

5. b.)  $y = -2 \cos(4x - \pi/2) + 3$   
 period (P) =  $\frac{2\pi}{|B|} = \frac{2\pi}{4} = \pi/2$

critical point =  $\frac{\pi}{2} \div 4 = \pi/8$

Amplitude = -2

vertical displacement = 3



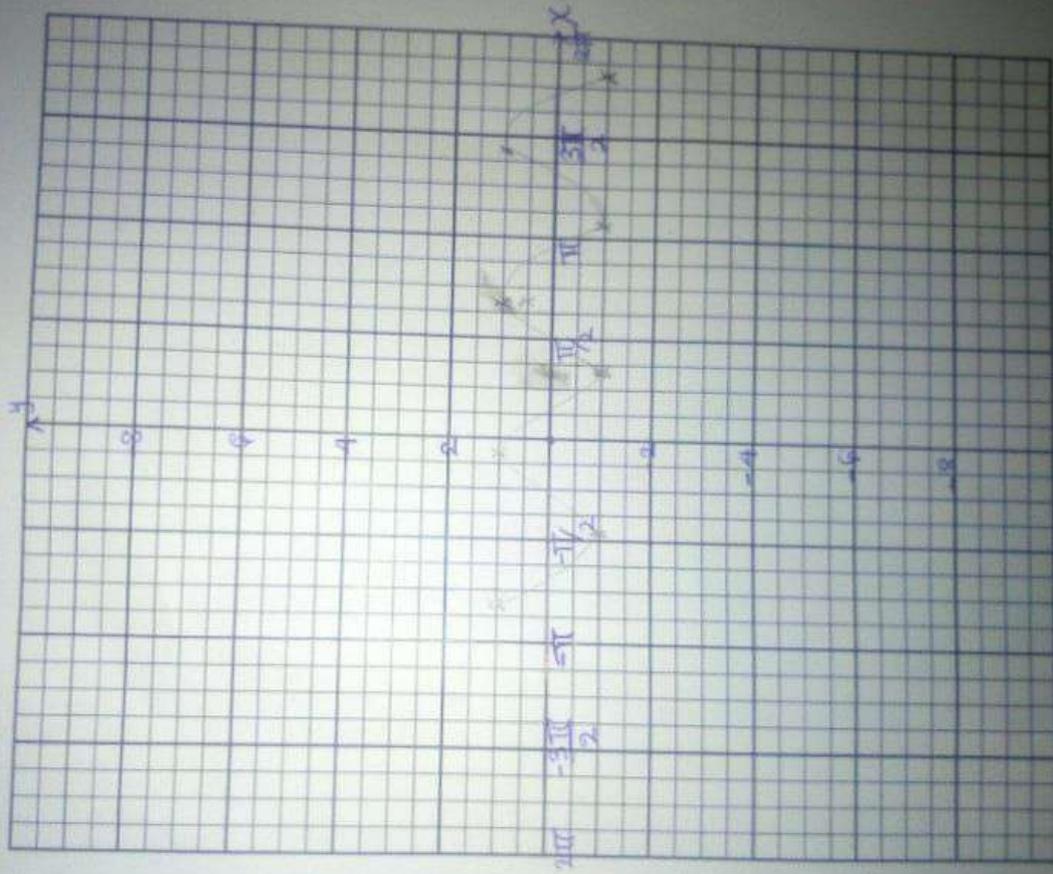
15. a)  $y = \sin(x + \pi/8) - 1$

Period  $(P) = \frac{2\pi}{|B|} = \frac{2\pi}{1} = 2\pi$

Critical points  $= \frac{2\pi}{4} = \pi/2$

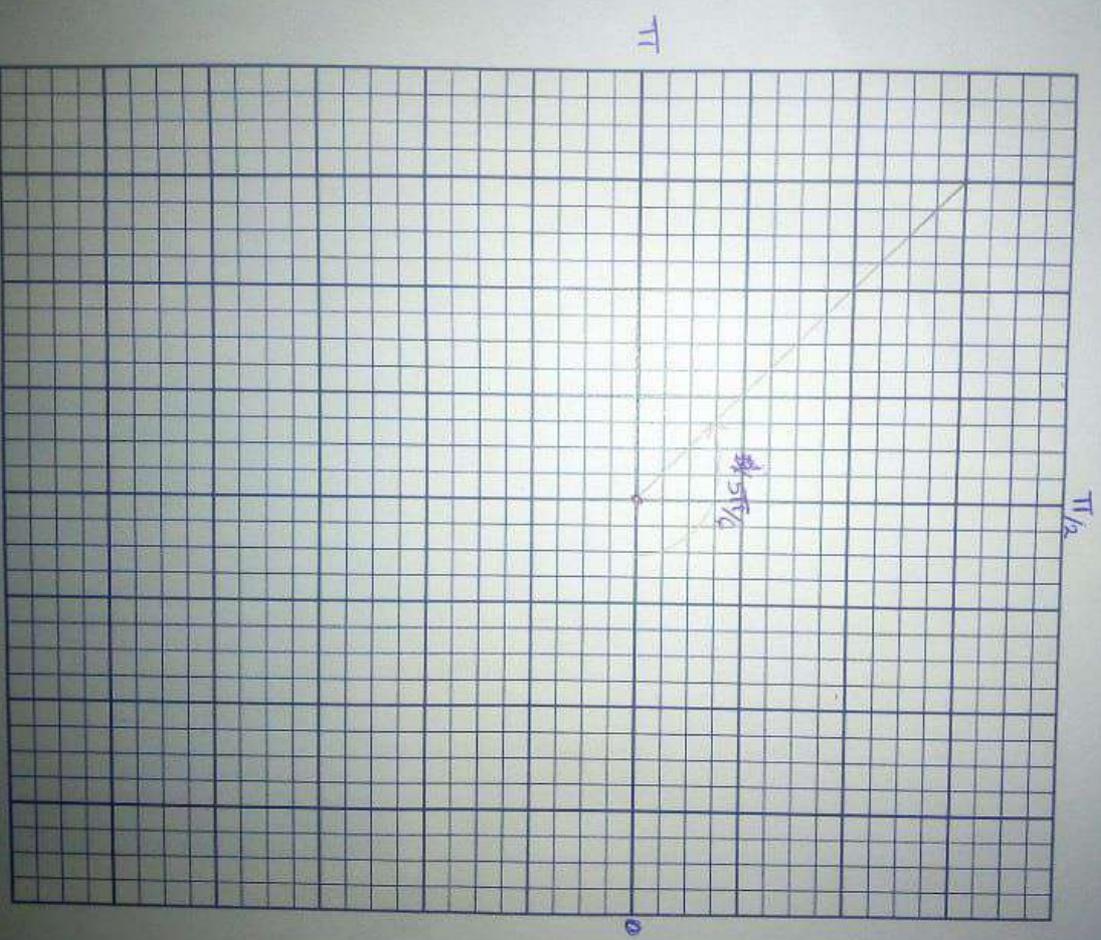
Amplitude  $= 1 \neq -1$

Midpoint  $= -1$



9. a)  $\cot \frac{5\pi}{6}$   
 $\cot \frac{5\pi}{6} = \frac{\cos(\frac{5\pi}{6})}{\sin(\frac{5\pi}{6})}$

$\cos(\frac{\pi}{6}) = \frac{\sqrt{3}}{2}$   
 $\sin(\frac{\pi}{6}) = \frac{1}{2}$



$-\frac{\sqrt{3}}{2} \times \frac{2}{1} = -\sqrt{3}$

15. a)  $y = \sin(x + \pi/8) - 1$  Midpoint = -1

Period  $(p) = \frac{2\pi}{|B|} = \frac{2\pi}{1} = 2\pi$

Critical points =  $\frac{2\pi}{4} = \pi/2$

Amplitude = 1  $\neq$  -1

